

## 1. MATRICES

## 1.1. Example 1.

$$\begin{pmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{pmatrix}$$

## 1.2. Example 2.

$$\begin{aligned} \begin{vmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \end{vmatrix} &= 1 \cdot \begin{vmatrix} 1 & 1 \\ 0 & 1 \end{vmatrix} - 0 \cdot \begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix} + 1 \cdot \begin{vmatrix} 1 & 0 \\ 1 & 1 \end{vmatrix} \\ &= 1 \cdot 1 + 1 \cdot 1 \\ &= 2. \end{aligned}$$

1.3. **Example 3.** Consider the matrix  $\alpha = \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix}$ . Observe that for any integer  $n$  we have

$$\alpha^n = \begin{pmatrix} 1 & n \\ 0 & 1 \end{pmatrix}.$$

## 2. ALIGNING EQUATIONS

Play with the following examples and create your own.

## 2.1. Example 1.

$$(1) \quad \sum_{m=1}^{\infty} \frac{c_m}{m^\nu} \sqrt{\left(\frac{2}{m\pi x}\right)} \left\{ \cos\left(mx - \frac{1}{2}\nu\pi - \frac{1}{4}\pi - \eta_m\right) - \frac{4\nu^2 - 1}{8mx} \sin\left(mx - \frac{1}{2}\nu\pi - \frac{1}{4}\pi - \eta_m\right) \right\} + \frac{b_m}{m^\nu} \frac{(\frac{1}{2}mx)^{\nu-1}}{\Gamma(\nu + \frac{1}{2})\Gamma(\frac{1}{2})}$$

## 2.2. Example 2.

$$(2) \quad \sum_{m,n=0}^{\infty} e^{-a^n b^m x} = \frac{\log^2 x}{2 \log a \log b} + \log x \left( \frac{\gamma}{\log a \log b} - \frac{1}{2 \log a} - \frac{1}{2 \log b} \right) \\ + \frac{1}{12} \left( \frac{\log a}{\log b} + \frac{\log a}{\log b} + \frac{\pi^2 + 6\gamma^2}{\log a \log b} \right) - \frac{\gamma}{2} \left( \frac{1}{\log a} + \frac{1}{\log b} \right) + \frac{1}{4} \\ + \sum_{n=1}^{\infty} \frac{(-1)^n}{n!(a^n - 1)(b^n - 1)} + \frac{1}{\log a} \sum_{\substack{n=-\infty \\ n \neq 0}}^{\infty} \frac{\Gamma\left(-\frac{2n\pi i}{\log a}\right) x^{2n\pi i / \log a}}{1 - b^{2n\pi i / \log a}} \\ + \frac{1}{\log b} \sum_{\substack{n=-\infty \\ n \neq 0}}^{\infty} \frac{\Gamma\left(-\frac{2n\pi i}{\log b}\right) x^{2n\pi i / \log b}}{1 - a^{2n\pi i / \log b}}.$$